

# Cloud effective particle size and water content profile retrievals using combined lidar and radar observations

## 2. Comparison with IR radiometer and in situ measurements of ice clouds

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**Abstract.** A new combined lidar/radar inversion procedure has been developed for cloud effective radius and water content retrievals. The algorithm treats the lidar extinction, derived effective particle size, and multiple-scattering effects together in a consistent fashion. This procedure has been applied to data taken during the Netherlands Cloud and Radiation (CLARA) campaign and the Cloud Lidar and Radar Experiment (CLARE'98) multisensor cloud measurement campaign. The results of the algorithm compare well with simultaneous IR radiometer cloud measurements as well as with measurements made by using aircraft-mounted two-dimensional probe particle-sizing instruments.

### 1. Introduction

Recently, a new methodology for extracting cloud physical and optical properties from combined lidar and radar soundings was introduced. In our companion paper *Donovan and van Lammeren*, this issue, (hereinafter referred to as paper 1) it was shown that a combined lidar/radar equation may be formulated by parameterizing the lidar backscatter and extinction using the radar reflectivity together with the radar/lidar effective radius ( $R'_{\text{eff}}$ ). This equation can then be solved to yield lidar extinction and  $R'_{\text{eff}}$  profiles. In paper 1, it was also shown how water content and effective radius ( $R_{\text{eff}}$ ) profiles could be estimated if assumptions about the size distribution and (in the case of ice clouds) shape distribution of the cloud particles were made.

In paper 1 some sample applications of the procedure to radar and lidar data obtained during the

Dutch Clouds and Radiation (CLARA) campaign [*Van Lammeren et al.*, 1998] were presented. In this paper the strengths and weaknesses of the algorithm will be further illustrated by examining the application of the lidar/radar inversion procedure to data obtained during both CLARA and the Cloud Lidar and Radar Experiment (CLARE'98) [*Wursteisen and Illingworth*, 1999] multisensor cloud measurement campaigns. During both CLARA and CLARE'98, infrared (IR) radiometers were often operated alongside the lidars and radars. As an indirect check on the validity of the lidar/radar inversion procedure, for a number of suitable cases, the lidar-derived optical cloud properties are used as a basis for determining the downwelling 10.5- $\mu\text{m}$  irradiance using a radiative transfer model. The model results are then compared with observations made by using collocated 10.5- $\mu\text{m}$  radiometers.

In addition to the comparison with the IR radiometer observations, more direct comparisons with the results of in situ two-dimensional (2-D) particle sizing probes are made for some cases during CLARE'98. In particular, for a couple of overpasses, results derived using ground-based lidar (Vaisala CT-75K ceilometer) and radar data (GKSS Miracle Radar) are compared with 2-D aircraft-mounted probe results. In addition, On October 20 a near coincident flight path was flown by the French ARAT aircraft and the UK Meteorological Office (UKMO) C-130. The ARAT carried the LEAN-DRE 532-nm lidar along with the KESTREL 94-GHz radar. A comparison between the in situ and remotely derived lidar/radar results was conducted by using this data set.

In this paper, we will first briefly review the lidar/radar inversion procedure presented in paper 1. Following

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that, the application of the lidar/radar procedure to some illustrative examples taken from CLARA and CLARE'98 will be presented together with comparisons with the IR radiometer results. Next, comparisons between remotely derived cloud properties and in-situ measurements will be presented.

## 2. Lidar/Radar Inversion procedure

### 2.1. Lidar/Radar ratios

The lidar radar inversion procedure employed here has been extensively described in paper 1; so only a brief overview is given here. In brief, the procedure relies on using the radar reflectivity together with the lidar/radar effective radius ( $R'_{\text{eff}}$ ) to parameterize the lidar extinction. Considering solid spherical scatterers for the time being, we have

$$R'_{\text{eff}} = \left( \frac{\langle r^6 \rangle}{\langle r^2 \rangle} \right)^{1/4}, \quad (1)$$

where  $r$  is the particle radius and the braces indicate averaging over the cloud particle size distribution. If the cloud particles are large enough to be considered optical scatterers with respect to the lidar wavelength and at the same time can still be considered Rayleigh scatterers with respect to the radar wavelength then

$$\alpha_{\text{lid}} \propto \langle r^2 \rangle, \quad (2)$$

where  $\alpha_{\text{lid}}$  is the extinction coefficient at the lidar wavelength and

$$Z_e = \frac{\lambda_{\text{rad}}^4}{\pi^5} \left| \frac{n_w^2 - 1}{n_w^2 + 2} \right|^2 4\pi\beta_{\text{rad}} \propto \langle r^6 \rangle, \quad (3)$$

where  $Z_e$  is the radar reflectivity,  $\beta_{\text{rad}}$  is the backscatter coefficient at the radar wavelength ( $\lambda_{\text{rad}}$ ), and by convention,  $n_w$  is the complex index of refraction of water at 20°C. This implies that

$$\frac{Z_e}{\alpha_{\text{lid}}} \propto R'_{\text{eff}}{}^4 \quad (4)$$

regardless of the details of the size distribution. This will hold true whenever the particles are not so large they cannot be considered Rayleigh scatterers with respect to the radar wavelength nor so small that they cannot be treated as optical scatterers with respect to the lidar wavelength.

An exact treatment of ice crystals is not attempted here. Instead, the previous considerations may be approximately extended to the case of randomly orientated ice crystals. Since the lidar extinction will mainly depend on the cross-sectional area of the particles and the radar reflectivity will mainly depend on the square of the mass of the particles, we model ice clouds using distributions of equivalent  $R'_{\text{eff}}$  spheres. However, the

definition of  $R'_{\text{eff}}$  must be interpreted in terms of the mass and cross-sectional area of the particles such that

$$R'_{\text{eff}} = \left( \frac{9}{16\pi} \frac{\langle (M(D)/\rho_{s,i})^2 \rangle}{\langle A_c(D) \rangle} \right)^{1/4}, \quad (5)$$

where  $D$  is the maximum ice crystal dimension,  $M(D)$  is the ice crystal mass,  $\rho_{s,i}$  is the density of solid ice, and  $A_c(D)$  is the cross-sectional area of the particles. For the case of solid spherical particles where  $r$  has an obvious definition, then we have  $M(D)/\rho_{s,i} = 4/3\pi r^3$  and  $A_c = \pi r^2$ , and thus equation (5) reduces to equation (1). The idea of using equivalent  $R'_{\text{eff}}$  spheres is similar in concept to the idea of using equivalent  $R_{\text{eff}}$  spheres for modeling the absorption and scattering of ice crystals in the visible and IR [Grenfell and Warren, 1999]. However, the concept of using equivalent  $R'_{\text{eff}}$  spheres is different from the traditional approaches to modeling the radar wavelength scattering of nonspherical ice-crystals. The difference between using  $R'_{\text{eff}}$  and other equivalent sphere formulations (e.g., equivalent  $A_c$  or equivalent  $D$  spheres) will be discussed further in section 4 and Appendix A.

In order to interpret a measurement of  $R'_{\text{eff}}$  in an ice cloud and to estimate its ice water content (IWC), it is necessary to know or assume both the form of the ice crystal particle size distribution and the relationship between the particles cross-sectional area and mass. Suitable relationships between  $D$ , mass, and  $A_c$  have been compiled by Mitchell *et al.* [1996] and others.

### 2.2. Inversion Algorithm

Referring to Figures 4 and 5 of paper 1, it can be seen that there is a well-defined power law relationship (in terms of  $R'_{\text{eff}}$ ) between  $\alpha_{\text{lid}}$ ,  $\beta_{\text{lid}}$  and  $Z_e$ . Thus if the lidar extinction profile and the radar reflectivity profile are known, then  $R'_{\text{eff}}$  can be estimated. However, the lidar extinction must first be extracted from the lidar signal. The lidar signal is a function of both the lidar backscatter and extinction and can be written, assuming single scattering, as

$$P_{ss}(z) = C_{\text{lid}} z^{-2} \beta_{\text{lid}} \exp \left[ -2 \int_{z_0}^z \alpha_{\text{lid}}(z') dz' \right], \quad (6)$$

where  $z$  is the altitude,  $P_{ss}(z)$  is the returned single scattering power,  $\beta_{\text{lid}}$  is the backscattering coefficient at the lidar wavelength, and  $\alpha_{\text{lid}}$  is the corresponding extinction coefficient. Here  $C_{\text{lid}}$  is the effective calibration constant which takes into account fixed instrument parameters as well as the two-way attenuation loss suffered by the lidar signal between the lidar and  $z_0$ .

Let us neglect the contribution to the backscatter and extinction from molecular scattering. As discussed in paper 1, to reasonable approximation it can be assumed that  $\alpha_{\text{lid}} = B_\alpha Z_e R'_{\text{eff}}{}^{A_\alpha}$  and  $\beta_{\text{lid}} = B_\beta Z_e R'_{\text{eff}}{}^{A_\beta}$ . Equation (6) then becomes

$$S(z) \frac{(B_{\alpha_{\text{lid}}} Z_e)^A}{B_{\beta} Z_e} = C_{\text{lid}} \alpha_{\text{lid}}(z)^A \exp \left[ -2 \int_0^z \alpha_{\text{lid}}(z') dz' \right] \quad (7)$$

where  $S(z) = P_{ss}(z)z^2$  and  $A \equiv A_{\beta}/A_{\alpha}$ . Here  $Z_e$  is implicitly a function of range, while the coefficients (the  $A$ 's and  $B$ 's) depend to a first approximation only on whether the cloud particles are water or ice and are derived by using Mie theory.

The solution to equation (7) is given by

$$\alpha_{\text{lid}}(z) = \frac{[S'(z)/S'(z_m)]^{1/A}}{\frac{1}{\alpha_{\text{lid}}(z_m)} + \frac{2}{A} \int_z^{z_m} [S'(z')/S'(z_m)]^{1/A} dz'}, \quad (8)$$

where  $S'(z) = S(z)[(B_{\beta} Z_e)^A/(B_{\alpha} Z_e)]$  and  $z_m$  is some fixed boundary or normalization range.

Equation (8) is similar to the well known Klett solution form for the lidar equation [Klett, 1981]. However, equation (8) possesses the significant advantage of being able to employ a far-end boundary value determined by using the radar reflectivity and an estimate of  $R'_{\text{eff}}(z_m)$ , i.e.,

$$\alpha_{\text{lid}}(z_m) = B_{\alpha} Z_e(z_m) R'_{\text{eff}}(z_m)^{A_{\alpha}}. \quad (9)$$

**2.2.1. Determination of  $R'_{\text{eff}}(z_m)$ .** Choosing a particular value for  $R'_{\text{eff}}(z_m)$  implies a certain particular value for  $C_{\text{lid}}$  in equation (6). As described in paper 1, an automated procedure for determining  $R'_{\text{eff}}(z_m)$  near cloud top was developed. This procedure ensures that a value of  $R'_{\text{eff}}(z_m)$  is chosen such that the inferred value of  $C_{\text{lid}}$  is within a deemed physically reasonable range and that the gradient in the derived particle size profile around the normalization range is a minimum. Simulations have indicated that under a wide range of circumstances, this procedure finds a boundary value within 10-20% of the true value. For a discussion of the effect of an incorrect assignment of  $R'_{\text{eff}}(z_m)$  see paper 1, section 3.2 and Appendix B.

**2.2.2. Multiple Scattering.** For lidar cloud measurements, multiple scattering can significantly contribute to the observed signal. The magnitude of the multiple-scatter signal depends mainly on the angular width of the forward scattering lobe of the cloud particle's phase function compared with the field of view (FOV) of the lidar receiver. The width of the forward scattering lobe is, in turn, related to the cross-sectional area of the cloud particles. If multiple-scattering effects are neglected, the derived extinction will be less than the true extinction.

An approximate treatment of multiple-scattering effects has been incorporated into the inversion process. As described in paper 1, an iterative correction for multiple scattering is used in the inversion procedure. The procedure relies on the approximate multiple-scatter

model due to *Eloranta* [1998] which performs best for large particles (i.e., strong forward scattering).

### 3. Comparison with IR radiometer results

During CLARA an IR radiometer was in constant operation alongside the lidars and the Delft 3-GHz radar. The Royal Netherlands Meteorological Institute (KNMI) IR radiometer measures the sky brightness temperature using a IR passband of 9.6-11.5  $\mu\text{m}$ . It is an unattended instrument reporting minimum, maximum and average sky brightness temperature data every 60 s. The lidars and the radar system used during CLARA were described in paper 1.

As an indirect test of the results of the lidar-radar-derived IWC and particle size profiles, the inversion products were used as a basis for predicting the downwelling 10.5- $\mu\text{m}$  irradiance which were then compared with actual IR radiometer observations. As a first step, the retrieved optical properties at the lidar wavelength were extrapolated to 10.5  $\mu\text{m}$ . The optical properties at 10.5  $\mu\text{m}$  were then used in a radiative transfer model to predict the downwelling thermal irradiance and then compared with the IR radiometer observations.

For an idealized homogeneous nonscattering cloud layer the directly downward irradiance (neglecting gaseous absorption and emission) will be given by

$$I(\pi)_{9.6-11.5} = \int_{9.6}^{11.5} B(\lambda, T) \epsilon(\lambda) d\lambda, \quad (10)$$

where  $B(\lambda, T)$  is the blackbody radiance at temperature  $T$  and wavelength  $\lambda$  and  $\epsilon(\lambda)$  is the emissivity. If we assume that  $\epsilon(\lambda)$  is approximately constant within the spectral window, then

$$I(\pi)_{9.6-11.5} \approx \epsilon B(T), \quad (11)$$

where

$$B(T) = \int_{9.6}^{11.5} B(\lambda, T) d\lambda. \quad (12)$$

The average emissivity  $\epsilon$  is in turn a function of the absorption optical depth of the cloud layer, e.g.,

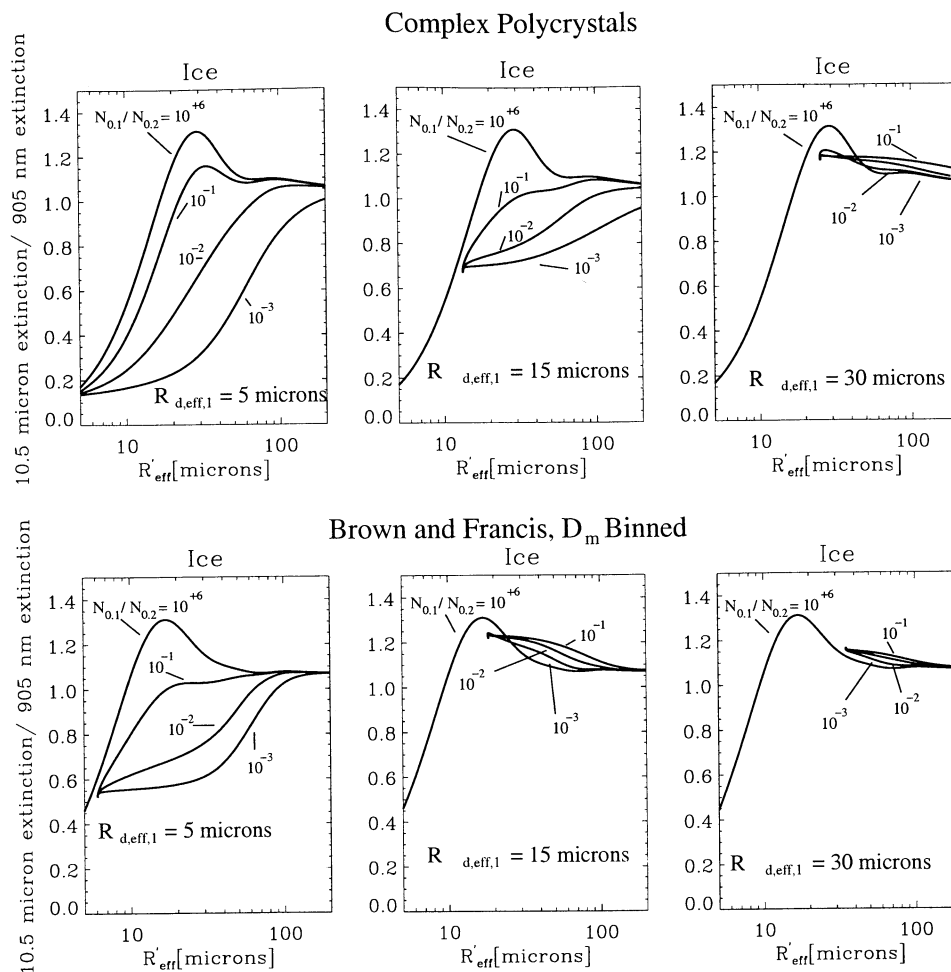
$$\epsilon = 1.0 - \exp(-\tau_{\text{abs}}), \quad (13)$$

where

$$\tau_{\text{abs}} = \int_{z_1}^{z_2} \alpha_{10.5\mu\text{m}}(z') (1.0 - \omega_{10.5\mu\text{m}}(z')) dz', \quad (14)$$

where  $z_1$  is the cloud base,  $z_2$  is the cloud top, and  $\omega$  is the single-scattering albedo of the cloud particles.

To accurately model real atmospheric cases, it is necessary to take into account such factors as gaseous absorption and emission, as well as nonhomogeneous cloud



**Figure 1.** Ratio of 10.5- $\mu\text{m}$  extinction to 905-nm extinction for a number of different families of bimodal gamma type cloud particle size distributions (see equation (23) in paper 1) for two different ice crystal habits.

optical properties and temperature variations within the cloud. However, the dominant factor is the correct specification of the cloud 10.5- $\mu\text{m}$  absorption optical depth. This quantity may be inferred by using the lidar/radar inversion results as a starting point. If the particles are sufficiently large, then they may be regarded as optical scatterers/absorbers at both 10.5  $\mu\text{m}$  and 905 nm. The ratio of the extinction at both wavelengths will then be close to unity. For sufficiently large absorbing particles the single-scattering albedo will also approach 0.5. Thus if the cloud particles are large enough, then there will be no difficulty in extrapolating the 905-nm extinction to the extinction at 10.5  $\mu\text{m}$ . For ice cloud particle size distribution which contains sufficient fraction of particles whose maximum dimension is less than 10.5  $\mu\text{m}$  the relationship between the 10.5- $\mu\text{m}$  absorption and the 905-nm extinction will be more complicated.

The relationship between the 10.5- $\mu\text{m}$  extinction 905-nm extinction is explored in a quantitative sense in Figure 1 in which the ratio of the 10.5- $\mu\text{m}$  extinction to 905-nm extinction is shown for a number of cases. Here

we have assumed bimodal gamma type size distributions of the type described by equation (23) in paper 1. In each case, the values of  $N_{o,2}/N_{o,1}$ ,  $R_{d,eff,1}$ ,  $\gamma_1 = 10$ , and  $\gamma_2 = 4$  were fixed while  $R_{m,2}$  was varied. Results are shown for three values of  $R_{d,eff,1}$  (5, 15, and 30  $\mu\text{m}$ ) for four values of  $N_{o,2}/N_{o,1}$  ( $10^6$ ,  $10^{-1}$ ,  $10^{-2}$ , and  $10^{-3}$ ). The  $N_{o,2}/N_{o,1} = 10^6$  case represents the case of a virtually unimodal size distribution. The results shown are the product of Mie calculations applied to equivalent  $R_{eff}$  spheres for two different crystal habits (complex polycrystal *Mitchell et al.* [1996] and *Brown and Francis* [1995]  $D_m$  binned (see paper 1)). That is, each nonspherical particle in the size distribution is replaced by an appropriate number of solid ice spheres whose radius is such that both the crystal mass ( $M(r_d)$ ) and cross-sectional area ( $A_c(r_d)$ ) are preserved. It was demonstrated by Grenfell, and Warren [1999] who found that equal volume-to-area ratio spheres (equivalent  $R_{eff}$  spheres) can usefully model the infrared scattering and absorption properties of nonspherical ice particles.

Consistent with our aim of using the lidar-radar derived 905-nm extinction profile together with the lidar-

radar effective particle size measurements, the results are shown as functions of  $R'_{\text{eff}}$  (and not as functions of  $R_{\text{eff}}$ ). It can be seen that, as expected, the ratios converge for large values of  $R'_{\text{eff}}$ . However, how rapid the convergence is depends on the value of  $N_{o,2}/N_{o,1}$ ,  $R_{d,eff,1}$ , and the crystal habit. It can be seen, generally speaking, that for values of  $R'_{\text{eff}}$  greater than  $40 \mu\text{m}$  and values of  $N_{o,2}/N_{o,1}$  greater than  $10^{-2}$  the ratios are in the range of 0.9-1.1. For smaller values of  $R'_{\text{eff}}$ , the ratios are quite variable in the cases where  $R_{d,eff,1}$  is relatively small. Corresponding to Figure 1, the  $10.5\text{-}\mu\text{m}$  single-scattering albedo ( $\omega$ ) is shown as a function of  $R'_{\text{eff}}$  in Figure 2. The size distributions and crystal habits used here are the same as those used in the previous figure and the calculations were performed in a similar fashion. Here it can be seen that  $\omega$  generally varies between 0.4 and 0.5 for  $R'_{\text{eff}}$  greater than  $40 \mu\text{m}$  and  $N_{o,2}/N_{o,1}$  greater than  $10^{-2}$ . Putting the extinction ratio and single-scattering albedo results together implies that the conversion between 905-nm extinction and  $10.5\text{-}\mu\text{m}$  absorption can be reasonably carried out if  $R'_{\text{eff}}$  is greater than about  $40 \mu\text{m}$ . Below this value the exact form of the ice cloud particle size distribution becomes increasingly important.

A model based on a one-dimensional plane-parallel discrete ordinate radiative transfer equation solver (DISORT *Stamnes et al.*, [1988]) was constructed which calculates the  $9.6\text{--}11.5\text{-}\mu\text{m}$  sky zenith radiance based on the lidar/radar inversion results and a specified atmospheric gaseous composition and temperature profile. DISORT itself is a well-known radiative transfer equation solver for multiple-scattering and emitting layered media and is used as the core solver in packages such as MODTRAN [*Berk et al.*, 1989] and STREAMER [*Key and Schweiger*, 1998]. Once the relevant parameters are specified at each model level (in our case, layer optical depth, single-scattering albedo, scattering phase function, and temperature), then DISORT is used to solve the discrete ordinate form of the radiative transfer equation in order to obtain the downwelling vertical irradiance profiles. Thus factors such as the atmospheric transmission of the layer between the ground and the cloud, the emission of this layer, and the scattering of the infrared radiation by the cloud particles are all implicitly accounted for.

In this work, 16 streams were specified in the discrete ordinate calculations. A model level was specified every 100 m for altitudes below the cloud top along with

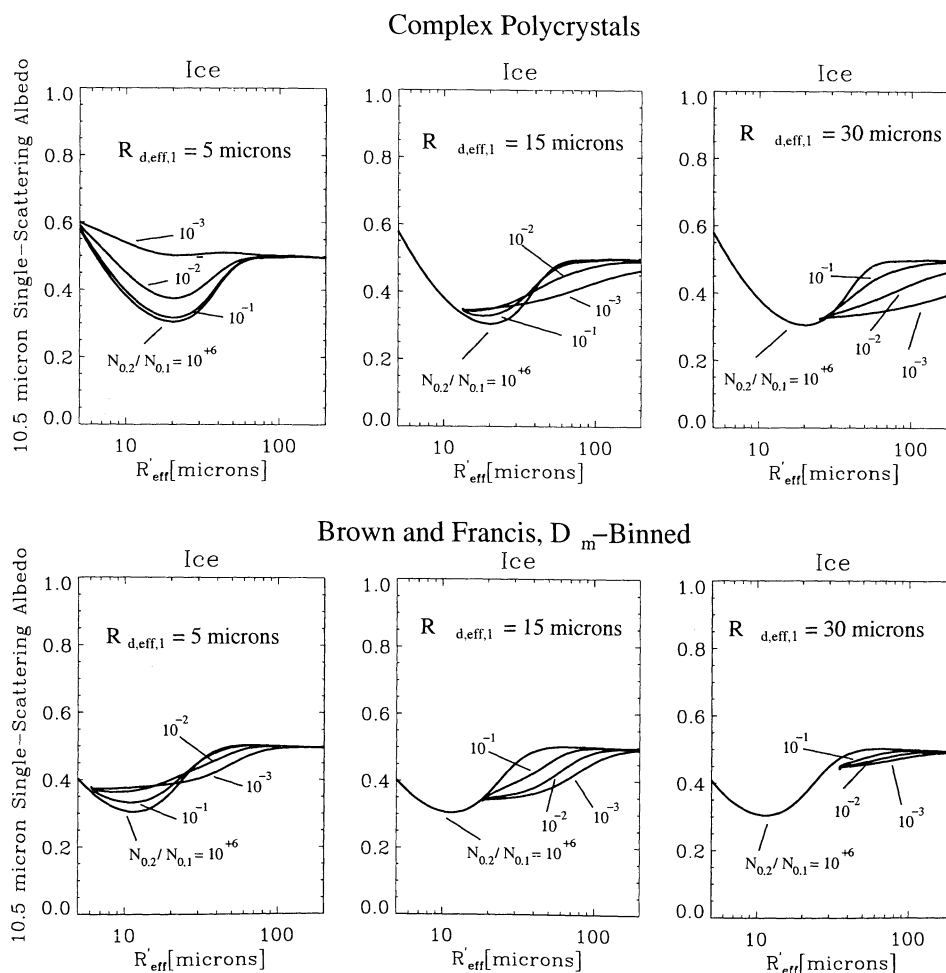
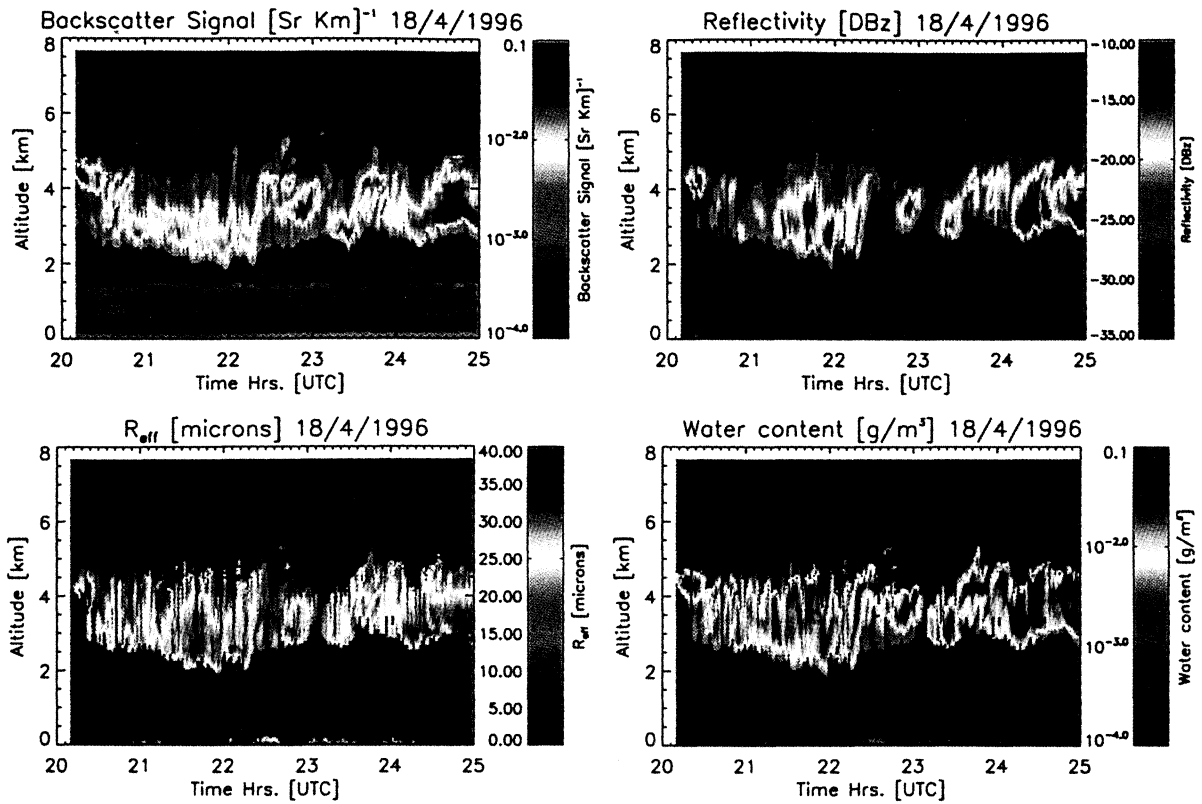
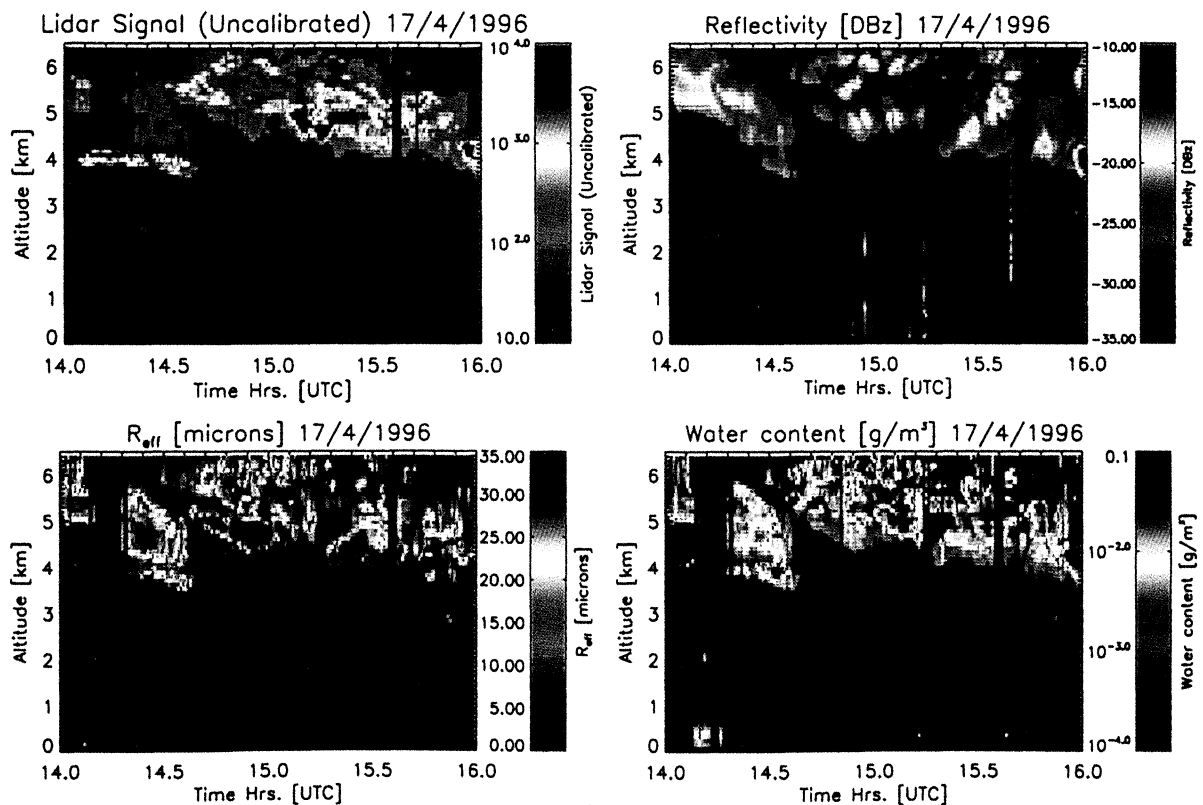


Figure 2. Single-scattering albedos corresponding to Figure 1.



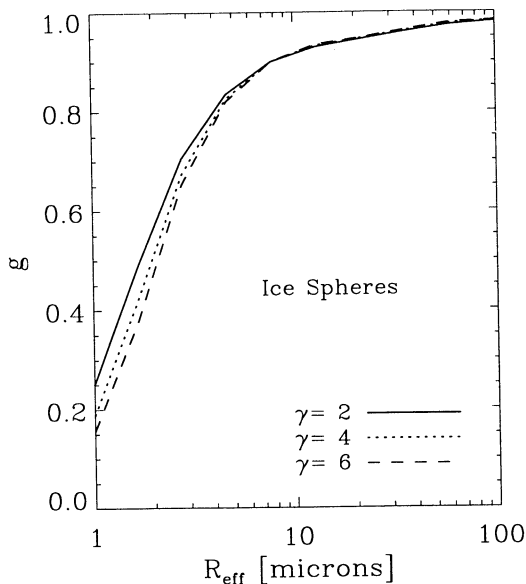
**Plate 1.** (top) Observed radar reflectivity and lidar backscatter signal together with (bottom) the results of the lidar/radar inversion for April 18, 1996.



**Plate 2.** (top) Observed radar reflectivity and lidar backscatter signal together with (bottom) the results of the lidar/radar inversion for April 17, 1996.

100 logarithmically spaced levels between the cloud top and 50 km. The model includes gaseous absorption and emission by water vapor,  $O_3$ , and  $CO_2$ . To find the gaseous optical depth for each layer, a Malkmus band model together with the two-parameter van de Hulst, Curtis, and Godson (H-C-G) approximation was used to account for the line absorption for  $O_3$  and  $CO_2$  [Goody and Yung 1989; Lenoble, 1993]. A Goody band model was used to treat the water vapor lines, while the water vapor continuum was handled by using the empirical formulas of Roberts *et al.* [1976]. The spectroscopic data used were taken from the tables compiled by Lenoble [1993]. The atmospheric temperature and humidity profiles used in the calculations for a particular instance of time were obtained by interpolating between profiles measured by locally launched radiosondes. The ozone mixing ratio profiles were taken from the climatology of Fortuin and Kelder [1998]. Emission from the ground was also accounted for. Consistent with a mixture of vegetation and damp ground, the ground emissivity was fixed at 0.95. For a discussion regarding the expected relative contribution of various processes (i.e., the importance of photons emitted by the ground and reflected by the clouds, etc.) the reader is referred to Platt [1973,1979], and Young [1995].

In order to account for the the scattering of thermal radiation by the cloud particles the phase function of the cloud particles must be approximated. Figure 3 shows the phase function asymmetry factor ( $g$ ) as a function of  $R_{\text{eff}}$  for a gamma size distribution of ice spheres. The results shown here were generated by using Mie calculations on spherical particles so that these results are only approximately true for irregular ice crystals Grenfell, and Warren [1999]. Nevertheless, it can be seen that for  $R_{\text{eff}}$  greater than 4-6  $\mu\text{m}$  the



**Figure 3.** Asymmetry factor ( $g$ ) as a function of  $R_{\text{eff}}$  for gamma distributions of ice spheres.

asymmetry factor is greater than 0.8, indicating that most of the scattering is in the forward direction. This implies that the effects of scattering will not be very important for clouds whose effective radius is above 4-6  $\mu\text{m}$  so it is not important for our purposes to get the details of the phase function right. This is fortunate, as general phase functions for ice crystals are not well known. Keeping this point in mind, for simplicity we choose to model the cloud phase function for ice clouds using Henyey-Greenstien functions, e.g.,

$$P_{\text{HG}}(\theta, g(z)) = \frac{1 - g(z)^2}{[1 + g(z)^2 - 2g(z) \cos(\theta)]^{3/2}}, \quad (15)$$

where  $\theta$  is the scattering angle and  $g(z)$  is the altitude dependent 10- $\mu\text{m}$  asymmetry factor inferred from the lidar/radar  $R_{\text{eff}}$  profile.

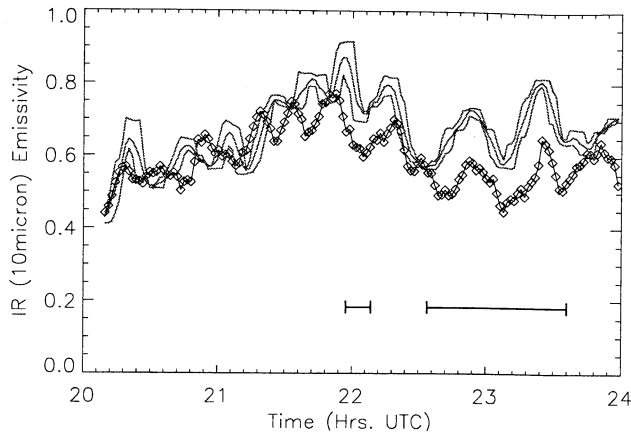
Referring to equation (11) and (13) it can be seen that for optically thick clouds ( $\tau_{10.5\mu\text{m}} > 4$ ) the amount of emitted radiation becomes dependent only on the cloud temperature itself. In order to usefully compare the lidar/radar results with the IR radiometer results, we will examine two ice cloud cases where the optical depth ranges between about 1 and 4.

### 3.1. April 18, 1996, CLARA

Sample radar reflectivity and lidar range corrected signal images are shown in the top panels of Plate 1 for April 18, 1996. Here the lidar data were acquired by using a Vaisala CT-75K 905-nm lidar ceilometer. The radar data were acquired by using the Delft 3-GHz radar and are shown in conventional units of dbZ where  $Z_e[\text{dbZ}] = 10 \log_{10} (Z_e[\text{mm}^6 \text{m}^{-3}])$ . Microwave radiometer measurements indicated that the maximum liquid water path was below 5  $\text{gm}^{-2}$  (the estimated minimum sensitivity of the instrument); so it was assumed that the cloud was composed of ice. By comparing the observed radar cloud top, and the apparent lidar cloud top it can be seen that the lidar signal usually penetrated the entire cloud deck and the radar registered the same cloud base as the lidar (or nearly so) before about 2200 UTC. After this time, periods where the lidar and radar cloud boundaries did not agree were present. Incidentally, it is interesting to note that below about 2.0 km the lidar observes boundary layer aerosol which is not detected by the radar.

The results of the lidar/radar inversion procedure applied to the data shown in the top panels of Plate 1 are shown in the bottom panels of Plate 1. In order to estimate the IWC and  $R_{\text{eff}}$  profiles from the retrieved  $R'_{\text{eff}}$  profiles together with the observed reflectivity profiles, a single-mode complex polycrystal model for the cloud particles was assumed [Mitchell *et al.*, 1996]. Here the retrieved  $R_{\text{eff}}$  values are mainly in the 25 to 30  $\mu\text{m}$  range and IWC values are mainly in the 0.02-0.05  $\text{gm}^{-3}$  range. The retrieved  $R'_{\text{eff}}$  values are in the range of 50-60  $\mu\text{m}$ .

Figure 4 compares the observed zenith effective cloud emmissivities (defined on the basis of the observed sky



**Figure 4.** Observed and calculated effective cloud 10.5- $\mu\text{m}$  emissivities for April 18, 1996. The triple lines show the maximum, average, and minimum IR radiometer observation within a 60-s time interval, while the dark line marked with squares shows results from the radiative transfer model using the lidar/radar inversion results. The solid line segments mark time periods where the lidar or radar cloud boundaries differed by 200 m or more.

radiances and the temperature at the observed cloud base) for April 18 with the results from the radiative transfer model using the lidar/radar inversion results. From 2000 to around 2200 UTC, the observed and calculated values agree within about 0.05. Using equations (11)-(14), this implies that the lidar-derived optical depth appears to be correct within about 15%. Later in the day the disagreement between the IR radiometer and the lidar/radar results grows to over 0.2. This is due mainly to parts of the cloud being below the radar's sensitivity (about -35 dBZ). As previously mentioned, before 2200 the lidar observed cloud boundaries are close to the observed radar cloud boundaries. After 2200 differences of up to 500 m are seen between the lidar- and radar-observed cloud boundaries. This highlights a weakness in the lidar/radar method, namely, that signals from both instruments must be present for the inversion to yield reliable results.

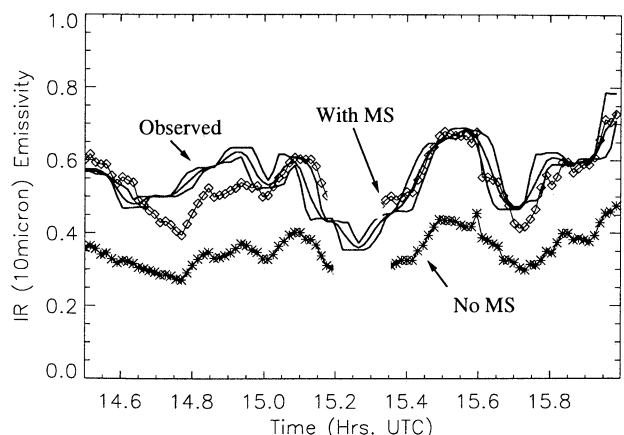
For this case the values of  $R'_{\text{eff}}$  were between 50 and 60  $\mu\text{m}$  so that according to our earlier discussion (see Figures 1 and 2) the ratio between the 10.5- $\mu\text{m}$  absorption and the 905-nm extinction is not very dependent on the particle size for monomodal distributions and for bimodal distributions if  $N_{o,2}/N_{o,1}$  is greater than about  $10^{-2}$ . Thus the agreement of our model calculations based on the lidar/radar retrieval results really only indicates that the derived 10.5- $\mu\text{m}$  optical depth is correct. This implies that the 905-nm optical depth derived by the lidar/radar procedure is correct to within 10-15%. In terms of particle size, though, the results only indicate that the particles were not smaller than  $R'_{\text{eff}} = 20\text{-}25 \mu\text{m}$  (otherwise the conversion between the 905-nm and 10.5- $\mu\text{m}$  extinction would have been no-

ticeably off). In short, the IR radiometer observations are consistent with the particle sizes inferred by the lidar/radar inversion, but not a rigorous test of the derived particle sizes.

### 3.2. April 17, 1996, CLARA

In contrast to the relatively homogeneous April 18 ice cloud example, a more structured mixed-cloud example is presented in Plate 2 (April 17, 1400-1530 UTC). The lidar data shown here were acquired by the Dutch National Institute of Public Health and the Environment (RIVM) Flight Temporal Resolution (HTRL) lidar at a wavelength of 1064 nm. Here there are several features present in the lidar image which are not present in the corresponding radar image. In particular, a layer present at 4.0 km between 1400 and 1430 UTC is clearly detected by the RIVM lidar but not by the radar. It is believed that the particles in this layer are too small to give rise to a usable radar signal; this implies that the layer had an effective radius below a few microns. Particles with radii this small may suggest the presence of supercooled water droplets. The temperature at 4.0 km was around  $-15^\circ\text{C}$ ; supercooled water layers may be observed down to temperatures of around  $-40^\circ\text{C}$ . Note also that this layer completely attenuates the lidar signals implying that its minimum optical depth is of the order of 4 at 1064 nm. Another area where the lidar detects cloud and the radar does not is present between 4.5 and 5.0 km at around 1510-1518 UTC.

The results of the inversion applied to the lidar and radar data are shown in the bottom panels of Plate 2. This example highlights the fact that retrievals are only possible when both the lidar and radar signals are above the noise floor. Here the retrievals are only representative of the entire cloud columns between about 1430-1512 and 1518-1548 UTC. During other times the presence of noise, attenuation of



**Figure 5.** Observed and calculated effective cloud emissivities for April 17, 1996. The area labeled "No MS" shows the computed emissivities when multiple scattering in the lidar signal is neglected.



the lidar signal, or the absence of a strong enough radar return made a representative retrieval impossible.

A comparison between the observed zenith sky radiance with the results from the radiative transfer model using the lidar/radar inversion results for April 17 is shown in Figure 5. As was discussed earlier, the retrievals are only representative of the entire cloud columns between about 1430 Hrs and 1548 UTC. Here it can be seen that good agreement is obtained for data taken past 1430 UTC. Note, that for this plot at around 1515 UTC, where the lidar has detected much more cloud in the column than the radar (see Plate 2) the lidar/radar data have not been plotted.

For the Vaisala lidar which has a small field of view (less than 0.5 mrad) there is generally only a small difference in the final results if multiple scattering is taken into account or not. However, the RIVM lidar has a large FOV (10 mrad); so multiple-scattering effects must be accounted for in the inversions. The lower line in Figure 5 shows the cases where the lidar/radar results derived by ignoring multiple scattering effects have been used to calculate the IR radiances. It can be seen that the agreement between the IR radiometer observations and the inversion results is notably degraded. The difference in the results stems mainly from the different cloud optical depths inferred when the inversion procedure accounts for multiple-scattering or not. If multiple scattering is ignored then the effective extinction is smaller than the real extinction (by up to a factor of 2 for large particles and large lidar fields of view). In addition, here the algorithm also tends to chose a different boundary value which results in an even lower retrieved extinction profile. The results shown in Figure 5 demonstrate the need to account for multiple-scatter effects in the retrievals and further support the manner in which we are accounting for multiple-scatter effects. More detail on the effects of multiple scattering on the inversion procedure can be found in paper 1.

#### 4. Comparison With In-situ Measurements

In this section, comparisons between the C-130 2-D probe measurements and the results of both ground and aircraft based lidar/radar cloud soundings are presented for two days during the CLARE'98 campaign. CLARE'98 was conducted during October 5-23, 1998, at the Chilbolton Observatory, Hampshire, UK [Wursteisen and Illingworth, 1999]. For two overflights of the UK Meteorological Office (UKMO) C-130 on October 21, results are shown which use the combination of the ground-based GKSS 94-GHz radar [Danne and Quante, 1999] and the Vaisala CT-75K 905-nm lidar ceilometer [Goddard, 1999]. For October 20, comparisons between the lidar/radar inversion results using the airborne KESTREL 94-GHz radar together with the LEANDRE 532-nm lidar (both mounted on the

ARAT aircraft) and in situ measurements made during a near-coincident C-130 flight are presented. Details of the LEANDRE radar and the KESTRAL lidar instruments can be found in the work of Pelon *et al.* [1999] and Guyot *et al.* [1999] respectively. For the 94-GHz CLARE data that are presented in this work, the gaseous attenuation was calculated from the UKMO Unified Model output and using the model of Liebe [1985], while the temperature dependence  $K_w$  was calculated by using the approach of Liebe *et al.* [1989].

During CLARE'98, several flights of the UK meteorological office C-130 aircraft were conducted [Francis, 1999]. The C-130 mounted several in situ particle sizing instruments including 2-D Cloud (2D-C) and 2-D Precipitation (2D-P) probes. The probes are based on the instrument described by Knollenburg [1970] and basically consist of a laser which illuminates a linear array of 32 photodiodes; as hydrometeors pass through the sample volume, they cast a shadow on one or more of the diodes and enable a two-dimensional image to be compiled from which size and shape can be determined. The 2D-C probe detects particles in the size range 25–800  $\mu\text{m}$ , and the 2D-P probe detects particles in the range 200–6400  $\mu\text{m}$ . From each crystal image both the area ( $A_c$ ) and the mean of the maximum crystal dimensions measured parallel and perpendicular to the photodiode array ( $D_m$ ) are calculated. Crystal size spectra are then computed as functions of both  $A_c$  and  $D_m$  for each 5 s segment of data.

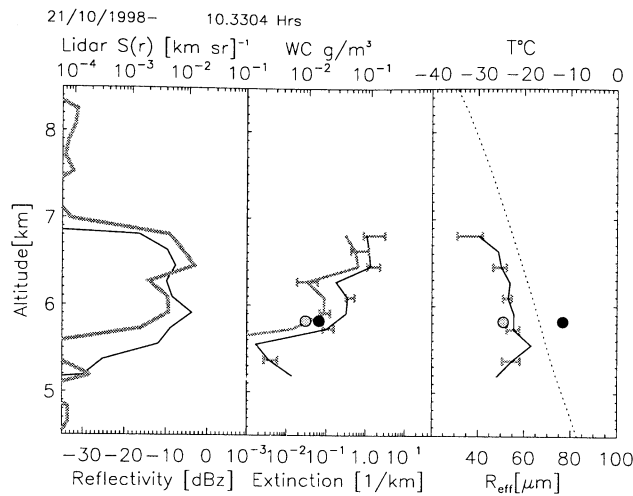
Two different methods for estimating the crystal masses from the 2-D results have been used. One method parameterizes the crystal mass according to its value of  $D_m$ ; the other parameterizes the crystal mass according to its value of  $A_c$ . These two methods agree for small crystal sizes but diverge for crystals with  $D_m$  greater than about 100  $\mu\text{m}$ . The two different relationships give a different mass versus area relationship and thus imply different  $R'_{\text{eff}}$  versus  $R_{\text{eff}}$  relationships. For the purpose of interpreting the radar reflectivity the relationship between  $R'_{\text{eff}}$  and  $R_{\text{eff}}$  is important, since, as was shown in paper 1, the IWC is proportional to the reflectivity and  $R_{\text{eff}}/R'_{\text{eff}}$ , i.e.,

$$\text{IWC} = \rho_{s,i} \frac{\pi}{48} \left( \frac{|K_w|}{|K|} \right)^2 \left( \frac{R_{\text{eff}}}{R'_{\text{eff}}} \right) \frac{Z_e}{R_{\text{eff}}^3}, \quad (16)$$

where  $\rho_{s,i}$  is the density of solid ice. A comparison of the  $R'_{\text{eff}}$  to  $R_{\text{eff}}$  ratio as a function of  $R'_{\text{eff}}$  for several ice crystal habits was shown in paper 1, Figure 10. There the relationships implied by the two different methods of interpreting the 2-D spectra are compared with those implied by the various models used by Mitchell *et al.* [1996].

##### 4.1. October 21, 1998, CLARE'98

On this day the UKMO C-130 passed over the Chilbolton site four times. Two of the over passes



**Figure 6.** (left) Lidar (light solid line) and radar (heavy solid line) signal profiles for October 21, 1996, at 1020 UTC. (middle) Retrieved 905-nm extinction profile (heavy solid line) and estimated IWC profile (light solid line). (right) Retrieved  $R_{\text{eff}}$  profile and the UKMO temperature profile (dotted line, upper axis). Solid circles denote values inferred from the C-130 mounted 2-D probes using the mass-versus-area relationship, while the shaded circles show the respective estimate made by using the mass-versus-maximum average dimension relationship.

occurred around 1020 UTC and two occurred around 1050 UTC. Throughout the campaign a ground-based Vaisala CT-75K 905-nm lidar was in continuous operation. During the aircraft flight times, the GKSS 94-GHz radar and the Rablles 35-GHz radar were mainly operating in a scanning mode, but they also obtained vertically pointing “snapshots” around the direct overpass times. Here the GKSS radar data were chosen for comparison with the lidar due to the higher spatial resolution of the data.

The Vaisala CT-75K lidar signal and the equivalent reflectivity observed by the GKSS radar are shown in Figure 6. The radar signal here is a snapshot of around 10 s, while the lidar signal is an average of about 1.5 min. The raw CT-75K measurements have a temporal resolution of 30 s, and averaging beyond this was found to be necessary. This was due to the relatively low signal-to-noise ratio of the lidar signal and the sporadic detection of the cloud layer between 5.5 and 7 km by the lidar ceilometer. Figure 6 also shows the ice water content and  $R'_{\text{eff}}$  profiles derived for the lidar and radar signals together with the values estimated for the IWC and effective radius from the 2-D probe data at around 5.8 km during the overpass.

The lidar-radar derived IWCs and  $R_{\text{eff}}$  values were estimated from the reflectivity profiles along with the derived  $R'_{\text{eff}}$  profile assuming the  $D_m$  binned model relationship between particle mass and cross-sectional area of Francis *et al.* [1998], while the 2-D probe estimates shown were made by using both the  $D_m$  binned and  $A_c$

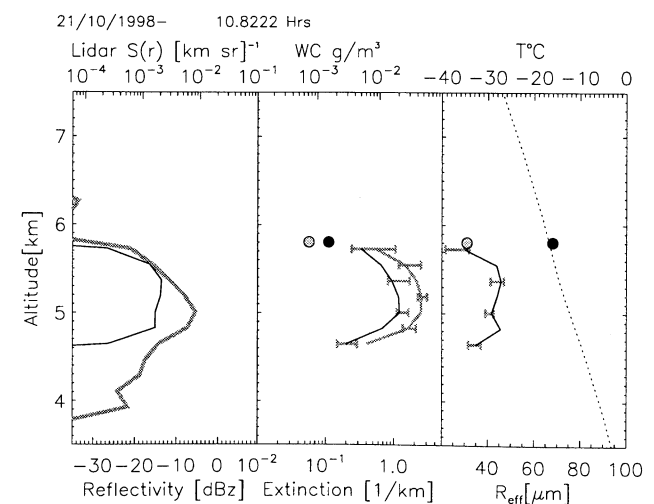
binned relationships. These two methods tend to agree for smaller particles but diverge for larger particle sizes. It can be seen that the values for the ice water content estimated using the lidar-radar inversion are consistent with the 2-D probe estimates. In this figure it can be seen that the effective radii estimates at 5.8 km seem consistent within their respective uncertainties.

The results for a later overpass are shown in Figure 7. Here it appears that the aircraft sampled near the top of the cloud. The agreement here is seen to be not as good as that for the earlier overpass. In particular, the aircraft appeared to fly just over the top of the observed cloud; also in this case there is a 30-s delay between the lidar/radar data and the actual overpass time. Either of these two effects may account for the apparent mismatch between the 2-D probe and lidar/radar IWC values. However, the agreement between the particle sizes appears to be quite good. Here it can be seen that the observed particle sizes are smaller than those measured for the previous overpass for the higher cloud layer.

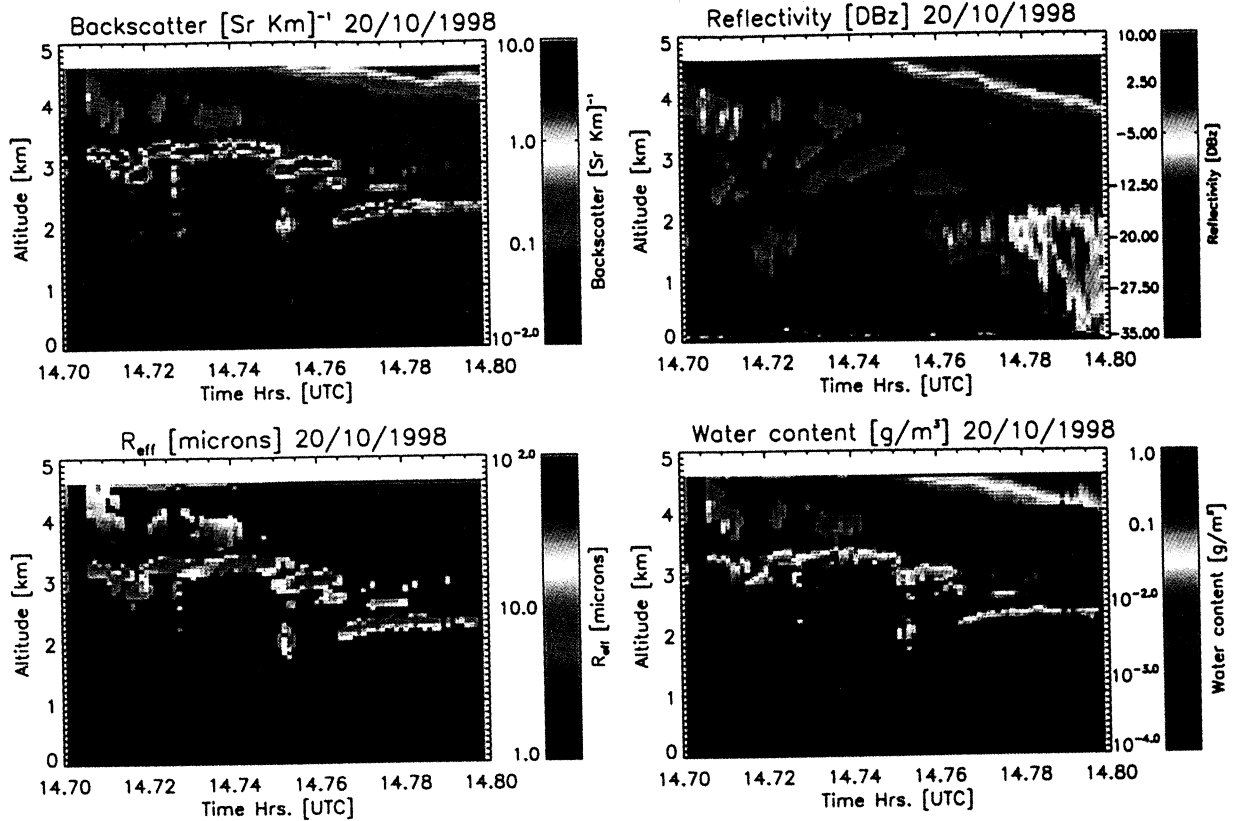
#### 4.2. October 20, 1998

On October 20 a near-coincident flight path was flown by the French ARAT aircraft and the UKMO C-130. The ARAT carried the LEANDRE 532-nm lidar along with the KESTREL 94-GHz radar. The observed reflectivities and backscatter signals for this flight are shown in the top panels of Plate 3. A large cloud is visible in the top right portion of both panels, while the lidar image shows several strong backscattering layers not prominent in the radar reflectivities. These layers attenuate the lidar returns so that no useful lidar signal is present below about 2.0 km.

The bottom panels of Plate 3 show the estimated lidar/radar effective particle size and the estimated water contents. The C-130 flights on this day show that layers of liquid water were often present over and around Chilbolton. However, little water was encountered during the coincident C-130 flight at 4.6 km. The inversion



**Figure 7.** Same as Figure (6) except for 1049 UTC.



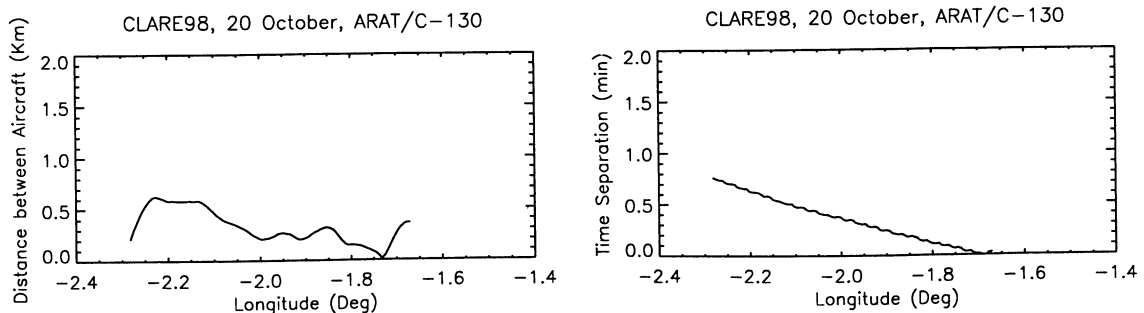
**Plate 3.** (top) Observed radar reflectivity and lidar backscatter signal together with (bottom) the results of the lidar/radar inversions for the ARAT flight path.

results shown here were conducted by assuming that the strong backscattering layers below about 3.25 km ( $T = -4^{\circ}\text{C}$ ) were composed mainly of liquid water, while elsewhere it was assumed that the clouds were ice. If an inversion is conducted by assuming ice everywhere, then the inferred particle sizes in these layers are still quite small (less than  $2\text{--}4\ \mu\text{m}$ ). Since the far-end boundary values used in the inversions were set at the altitudes of these layers, assuming they are mainly ice instead of water alters the particle sizes and IWCs inferred for altitudes closer to the aircraft by not more than 10–20%.

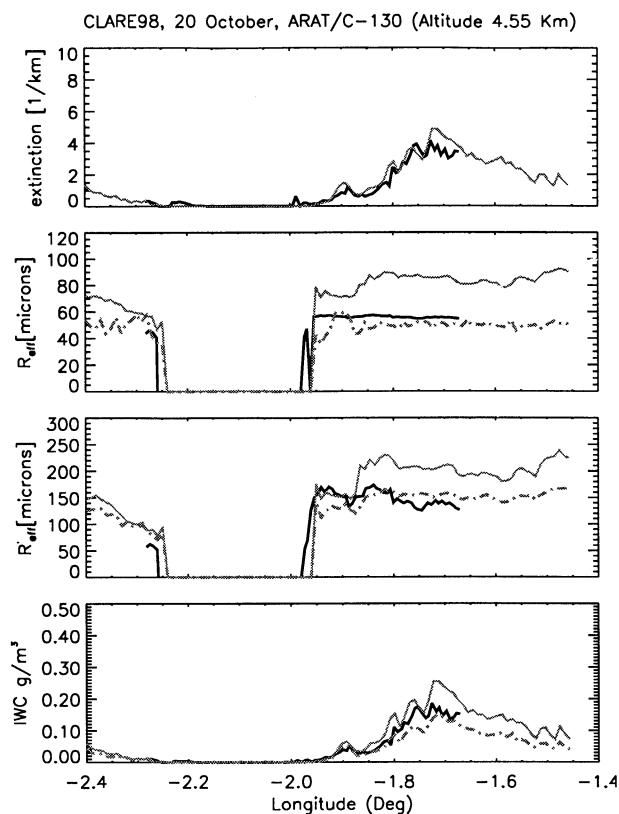
The separation in space and time as a function of latitude between the ARAT and the UKMO C-130 are shown in Figure 8. It can be seen that within about

10 km of Chilbolton the horizontal separation of the two aircraft was within 300 meters and the time difference within half a minute. Such separations are not ideal, but given the large extent and high apparent stability of the large ice cloud sampled here together with the horizontal resolution of the aircraft measurements (about 500–600 m for the C-130 measurements), they may be considered adequate for useful comparison in this case.

A comparison between various cloud properties inferred from the 2-D probe measurements and the lidar/radar inversion results is shown in Figure 9. The lidar/radar results shown are for an altitude of 4.55 km, which was the maximum height at which reliable data



**Figure 8.** Separation in space and time between the ARAT and the UKMO C-130 as a function of longitude.



**Figure 9.** Comparison of lidar/radar results and 2-D probe results for the ARAT/C-130 flight path. Heavy solid lines show the respective results from the lidar/radar inversions at 4.55 km. Light solid lines show the respective results for the 2-D probe data using the mass-versus-area relationship, while the dot-dashed lines show results of the mass-versus-maximum average dimension relationship.

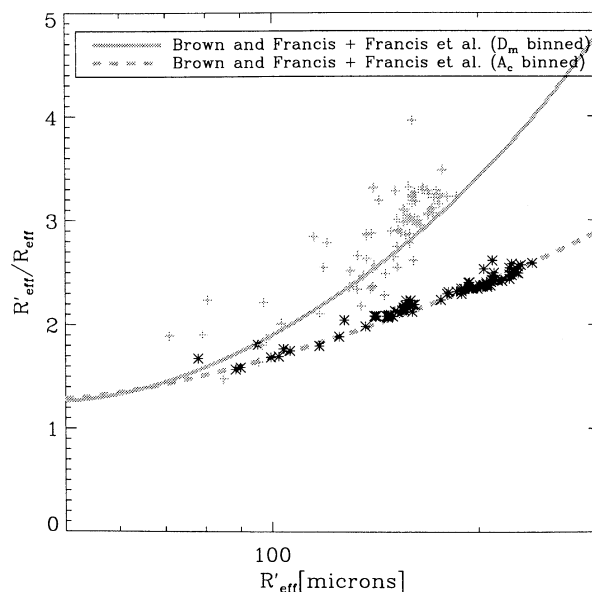
were obtained. The ARAT flew at an altitude of about 4.85 km, while the C-130 flew at an altitude of around 4.6 km, which is just slightly higher than the maximum height of reliable lidar/radar data but is within one range bin (the resolution of the lidar data was 60 m) of the top of the lidar/radar data. As was the case for the ground-based October 21 results, results for the two different ways of interpreting the 2-D probe data are presented except for the case of the inferred extinction. Since the optical extinction inferred from the 2-D probes is just twice the cross-sectional area of the particles, the area-binned 2-D probe results for extinction are considered to be more accurate than those that may be inferred from the average dimension spectra. The lidar/radar IWC and  $R_{\text{eff}}$  estimates shown here were generated by using the  $D_m$  binned model and assuming that the particle size distribution could be described by a gamma-type function with  $\gamma = 2$ . A comparison between the values of  $R'_{\text{eff}}/R_{\text{eff}}$  inferred from the 2-D probe data and theoretical values based on gamma size distributions is shown in Figure 10. Both the “observed” values of the ratio and the theoretical values depend on

the set of assumed mass to  $D_m$  and area to  $D_m$  relationships. However, it can be seen for both the  $A_c$  binned and the  $D_m$  binned methods of determining the particle masses that reasonable agreement could be achieved by using a monomodal size distribution with  $\gamma = 2$ .

Referring back to Figure 9 it can be seen that the comparisons between the lidar-radar-derived quantities and the 2-D probe measurements are consistent within the uncertainty between the two methods for determining particle mass from the 2-D probe measurements. In particular, the lidar/radar results for IWC appear to agree somewhat better for most of the flight path with the  $D_m$  derived 2-D probe estimates. The significance of this result is unclear at this point. The lidar/radar estimate of  $R'_{\text{eff}}$  and extinction are the fundamental products of the inversion and are not dependent on the assumed crystal habit. However, the 2-D probe estimates of  $R'_{\text{eff}}$  are dependent on the assumed crystal-habit. It is quite encouraging that the lidar/radar  $R'_{\text{eff}}$  time series agrees well with one of the methods for interpreting the 2-D probe data, but it remains to be seen whether such agreement is to be commonly expected or is limited to certain special circumstances. Further flight data, in connection with an independent measure of the IWC, are needed to truly verify the accuracy of the lidar/radar method as well as to better interpret the 2-D probe measurements themselves.

## 5. Summary and Conclusions

In this paper we have presented evidence that the lidar/radar inversion algorithm described in detail in paper 1 generates results which compare well with ground-



**Figure 10.**  $R'_{\text{eff}}/R_{\text{eff}}$  inferred from the 2-D probe data using both the  $A_c$  binned and the  $D_m$  methods. The lines show results that would be expected using gamma-type size distributions (in  $D_m$ ) with the width parameter  $\gamma$  equal to 2.

based passive remote sensing observations as well as with in situ aircraft-mounted particle probes. The agreement obtained between the lidar/radar results and independent IR radiometer observations and in-situ measurements presented here is very encouraging. In particular, the demonstration that the lidar/radar method results can be used to predict the 10.0- $\mu\text{m}$  surface irradiance demonstrates that the method yields the proper extinction within about 10%. This is supported by comparison with the area measurements of 2-D probe data. However, it is difficult to determine how accurate the IWC estimations are, owing to the fact that it is necessary to assume a crystal habit to interpret both the lidar/radar measurements and the 2-D probe measurements of mass. The agreement between the in-situ measurements and the lidar/radar measurements is encouraging. However, further comparisons with in situ measurements must be made under different cloudy conditions before firm conclusions concerning the accuracy of this method may be drawn. In particular, an independent measure of the IWC would be extremely useful. The possibility of conducting such measurements in the near future seems bright. The UKMO C-130 now mounts a Nevzorov hotwire probe [Korolev *et al.*, 1998] which provides a bulk measure of liquid water content and total condensed water content, from which ice water content can be derived. It is considerably more accurate than the bulk measure provided by Brown's [1993] total water probe, which measures the total water content including vapor and then subtracts the components that are not ice using other bulk measurements.

Despite these reservations it should be noted that the lidar/radar method developed in paper and demonstrated in this paper represents a significant advancement with regard to active remote sensing of clouds. By using the radar and lidar signals together the procedure, to a large degree, overcomes the problem of accurately extracting the extinction from the lidar signal, while at the same time it accounts for multiple scattering. With respect to cloud remote sensing this procedure demonstrates the power of combining the lidar and radar measurements together within a consistent framework. However, further work will be necessary to quantify the accuracy and the range of validity of the assumptions inherent in the method.

## Appendix A: Calculation of $Z_e$

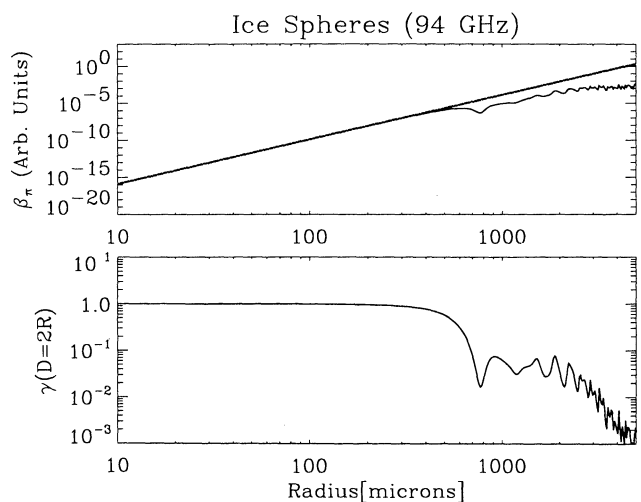
The problem of relating the radar reflectivity to the lidar extinction is very similar to the problem of predicting  $Z_e$  from 2-D images of particle area (extinction). Thus we have used the 2-D probe data alone to explore the consequences of using equivalent  $R'_{\text{eff}}$  spheres to model the cloud scattering properties. This method of modeling the particle scattering differs from previous approaches. Traditional approaches to calculating  $Z_e$  from 2-D particle size probe measurements assume that each single ice crystal can be modeled as a spherical ho-

mogeneous mixture of ice and air. Using equations (31) and (32) of paper 1, implies that in both cases, crystals smaller than around 0.1 mm are composed of solid ice, while at larger sizes inclusions of air result in a lower effective density. The reflectivity of a collection of these homogeneous spheres is then given by

$$Z = \sum_i \frac{|K(f_i)|^2}{0.93} n_i D_i^6 \gamma(D_i), \quad (\text{A1})$$

where  $D_i$  is the diameter of the equivalent sphere in corresponding to the  $i$ th size bin,  $n_i$  is the corresponding number density,  $\gamma(D)$  is the Mie/Rayleigh backscatter ratio, and  $|K(f)|^2$  is the "dielectric parameter" for a homogeneous ice-air mixture with an ice fraction  $f$  and is calculated by using the formulae of Meneghini and Liao [1996] and Liebe *et al.* [1989]. To a good approximation,  $|K|$  is proportional to  $f$ . For spectra binned by  $D_m$  we assume that the equivalent spherical diameter ( $D$ ) is equal to  $D_m$ , and for spectra binned by area we assume that  $D = D_{A_c} = 2(A_c/\pi)^{0.5}$ . The value of  $f$  for crystals in each size bin can then be calculated from equations (31) and (32) of paper 1. The factor of 0.93 is present in equation (A1) to make  $Z$  relative to liquid water at centimeter wavelengths. Both Brown *et al.* [1995] and Hogan and Illingworth [1999] have used this approach to calculate  $Z$  at 94 GHz from  $D_m$  binned aircraft size spectra.

An important point to note is that if a particular crystal is nonspherical, then in virtually every case, that  $D_m$  will be larger than  $D_{A_c}$ . This is because  $D_m$ , by its definition, represents in some sense an "envelope" that encloses the two-dimensional crystal image. As discussed in more detail later, both  $D_m$  and  $D_{A_c}$  will tend to be larger than the corresponding values of their equivalent

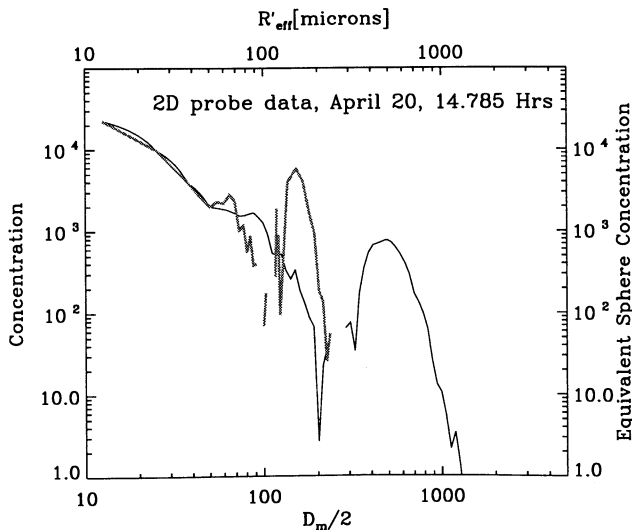


**Figure 11.** (top) Relative backscattering coefficient for solid ice spheres computed by using Mie theory (thin solid line) and the Rayleigh scattering approximation (solid thick line). (bottom) Ratio of Mie backscatter to that computed by using the Rayleigh scattering approximation.

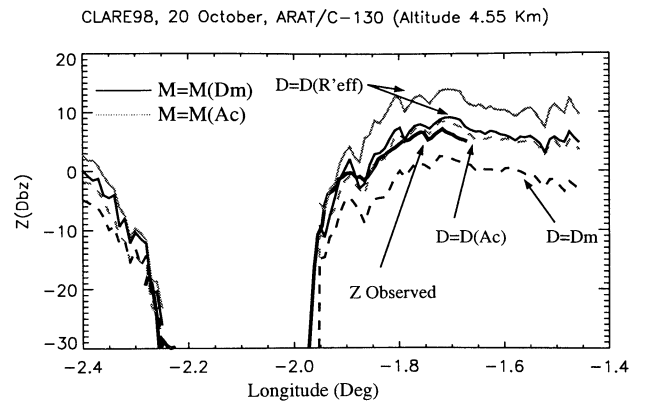
$R'_{\text{eff}}$  spheres. For small particles this poses no difficulty in calculating  $Z_e$  (where  $\gamma(D) = 1$ ) but creates uncertainty for larger particles. The variation of  $\gamma(D)$  with particle size is shown in Figure 11 for solid ice spheres at 94 GHz (if the spheres are not solid, the absolute value of the backscatter changes, but to a first approximation the general features of  $\gamma(D)$  are preserved). Here it can be seen that  $\gamma(D)$  falls very sharply for particles with radii greater than about 500  $\mu\text{m}$ .

The reduction in the magnitude of  $\gamma(D)$  with particle size has important implications for the calculation of  $Z_e$  when large nonspherical particles are present. This has been previously noted by Hogan *et al.* [2000] where  $\gamma(D)$  at the two wavelengths was exploited to infer crystal size using the combination of 35- and 94-GHz radar soundings of cirrus. If purely Rayleigh scattering is assumed and the masses are consistent, then the different equivalent sphere formulations will yield identical reflectivities. However, if Mie scattering is present, the different sizes of the different equivalent spheres will give different values for  $\gamma(D)$  and, thus, different values for  $Z_e$ . This effect can be illustrated by using the 2-D data.

For both the equivalent  $D_m$  and  $D_{A_c}$  spheres there is a one-to-one relationship between the number of ice crystals and equivalent spheres, and the density of the spheres is adjusted so as to give the proper mass. For the equivalent  $R'_{\text{eff}}$  spheres, the density is fixed (at that of solid ice), but the number density of the spheres is adjusted to give the proper second moment mass moment. That is, when calculating the scattering properties according to an equivalent  $R'_{\text{eff}}$  sphere hypothesis, each nonspherical particle in the size distribution is replaced by an appropriate number of solid ice spheres whose radius is such that both  $M(r_d)^2$  and  $A_c(r_d)$  are preserved so that



**Figure 12.** Comparison between merged 2-DC and 2-DP probe data shown as both number per  $D_m$  bin for  $D = D_m$  and equivalent  $R'_{\text{eff}}$  sphere number density.



**Figure 13.** Comparison between observed reflectivity for the October 20 overflight and reflectivities calculated from the 2-D probe data using equivalent  $R'_{\text{eff}}$  along with equivalent  $D_m$  and  $A_c$  spheres. Heavy solid lines show the results when the  $D_m$  binned mass is assumed (equation (31) of paper 1) while the light solid lines show the results when the  $A_c$  binned masses are used (equation (32) of paper 1).

$$n_{eq'}(r) = \frac{A_c(r_d)}{\pi r^2} n(r_d), \quad (\text{A2})$$

where  $r_d$  is half the particle maximum dimension (see section 2.3.2 of paper 1) and

$$r = \left( \frac{9}{16\pi} \frac{(M(r_d)/\rho_{s,i})^2}{A_c(r_d)} \right)^{1/4}.$$

Since the second moment of the mass and the area is preserved for each particle, these quantities will be preserved for the distribution as a whole. Hence the original distribution and the distribution of equivalent  $R'_{\text{eff}}$  spheres will have the same value of  $R'_{\text{eff}}$  as determined by equation (5).

Assuming equivalent  $R'_{\text{eff}}$  spheres has the effect of “shifting” the size distribution to smaller particles. This is demonstrated in Figure 12 where sample 2-D probe-measured spectra are plotted in terms of both concentration for equivalent  $D_m$  spheres and effective number density for equivalent  $R'_{\text{eff}}$  spheres. It can be seen that for small particles the concentration per bin is the same. However, for larger particles the  $R'_{\text{eff}}$  spectrum is shifted toward smaller particles. The shift toward smaller particles for the equivalent  $R'_{\text{eff}}$  spheres means for the April 20 2-D probe data that  $\gamma(D)$  is mainly close to unity for the equivalent  $R'_{\text{eff}}$  spheres while for both the  $D_{A_c}$  and  $D_m$  spheres this is not the case. This fact will lead to different calculated reflectivities. A comparison between the observed reflectivity along the ARAT flight path for the October 20 flight and the reflectivities calculated by using the 2-D data for equivalent  $R'_{\text{eff}}$  spheres with the masses given by both the  $A_c$  and  $D_m$  binned 2-D results along with  $D_m$  and  $D_{A_c}$  spheres is shown in Figure 13. Here it can be seen that the  $Z_e$  values calculated using the  $D_m$  spheres are too low by about

8 dbZ while the equivalent  $R'_{\text{eff}}$  spheres using the area-binned masses give reflectivities which are about 5 dbZ too high. However, both the  $R'_{\text{eff}}$  spheres using the  $D_m$  binned masses and the  $D = D_{A_c}$  spheres match the observed reflectivities within 1-2 dbZ.

Both matching methods here assume different masses for the ice crystals. Thus if an independent measure of the ice mass were available it would be possible to show whether the  $R'_{\text{eff}}$  spheres or the equivalent  $A_c$  spheres are most useful to model the reflectivity. Unfortunately, no such measurement was available. As was the case with the comparison between the 2-D results and the lidar/radar results, the results are very encouraging but not conclusive. The results, however, do support the consistency of the effective lidar/radar radius ( $R'_{\text{eff}}$ ) approach, which is an important concept in the the lidar/radar inversion procedure (see paper 1).

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