#### **Stochastic aspects of convection-permitting models**

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Scaling Cascades in Complex Systems 2017, Freie Universitat, Berlin 27–29 March 2017



### **Model filter**

- A numerical model of the atmosphere is based on a filter separating the flow into resolved and unresolved parts
- The purpose of parameterization is to feedback effects of the unresolved processes on the resolved state
- In general:
  - the feedback will depend on the nature of the filter
  - the feedback will not be a known deterministic function of the resolved state
- An ensemble-mean filter is deterministic
- A space/time filter might be approximated by sampling from possible physical realizations of the feedback from some conditional pdf



# **Ensemble mean parameterization**

#### Example case of scattered showers over UK



Radar image 1 (example from Adrian Lock)

#### 1.5km parameterized

#### 1.5km explicit



#### The grey zone

- For phenomenon of scale l and for  $\Delta$  a filter lengthscale...
  - if  $l \gg \Delta$  the phenomenon is well resolved
  - if  $l \ll \Delta$  the phenomenon is fully parameterized
  - if  $l \sim \Delta$  then the representation of the phenomenon is sensitive to details of the filter
- ▲ A spatially-averaged field on the scale ∆ may look turbulent but an ensemble-averaged field on that scale looks smooth
- What do we want our high-resolution models to produce?
  - a more detailed picture of the ensemble-mean flow?
  - a particular, possible realization of the actual flow?



# **Stochastic effects, reducing** $\Delta$

- GCMs have difficulties with organized convective structures where relevant interactions span a range of scales straddling  $\Delta$ 
  - talks by Khouider and Shutts
- For smaller  $\Delta \sim$  cloud spacing, then even scattered convection becomes stochastic because few clouds  $\Rightarrow$  poor sampling of the full pdf of possibilities



#### **Range of convective states**



Distribution of mass fluxes in equilibrium convection over ocean. Averaged over various areas.



### **Convection-permitting models**

- If  $\Delta \sim$  convective storm size, normal practice is to switch off deep convection parameterization
- Dynamical treatment of cloud assumed better than parameterized treatment
- Dynamics will be sensitive to details of filter, inc. grid length, numerics



# Stochastic effects, reducing $\Delta$

Uncertainties remain in the representation of deep convection that may be usefully addressed with stochastic approaches

- Shallow convection may be in a regime where  $\Delta \sim {\rm cloud}$  separation
  - talk by Seifert
- Initiation of dynamically-simulated deep convective clouds will depend on the state of the turbulent boundary layer



## **Turbulence parameterization**

- Our turbulence parameterization is formulated as an ensemble average
- Spatial-mean boundary-layer tendencies will vary randomly about that unless eddy size  $\not\ll \Delta$
- Largest, most vigorous eddies are responsible for initiating convective clouds and have size  $\sim h \sim$  cloud size  $\sim \Delta$
- ▲ ⇒ at just those ∆ where we might switch convection parameterization off, the boundary layer turbulence enters a grey zone where large eddies are poorly sampled by spatial averaging
- We need to contemplate a stochastic representation of the boundary layer



## **Gaussian bumps**

- Superposition of 2D Gaussian kernels applied to random number for each grid location,  $\sigma_x \sim 10 \text{ km}$
- Applied to potential temperature at a level within the boundary layer
- Every 30 min
- Small fluctuations  $\sim 0.1 {\rm K}$
- Cautious approach used in predictability studies







### **Impact of Gaussian bumps**

Number of ensemble members that are raining:



Small perturbations can easily shift the locations of precipitating cells in some cases



(Flack et al 2017)

## **Displacement of Convection**

Fraction of points that are raining in both of a pair of simulations



Equilibrium convection Non-equilibrium Equilibrium case saturates at 20% after  $\sim 20$  h, compared to 10% for completely random scatter through model domain



## **Implications I**

Testing changes to effects of other model settings needs to be done in an ensemble context.

	CDNC×2	CDNC×4
More rain	12	6
Less rain	24	30

Example of 6-member case study with enhanced cloud-doplet number concentration



# **Implications II**

Need to evaluate simulations against observations with more suitable metrics than point-to-point comparisons



e.g., spatial neighbourhood approaches that ask how much we have to coarse-grain the precipitation data to get agreement between two fields

(Dey et al 2016)



# **Summary of Gaussian bumps**

- Application can be anywhere in boundary layer
- Time/space correlations of modest effects only
- Amplitude of buoyancy perturbations applied is most important sensitivity
- Perturbations produce earlier initiation (may be a major motivation for their introduction)
- Dynamics of convective cells largely unchanged: may be displaced and *could* increase number



### **BL** scaling

The turbulent boundary layer under deep convective storms is itself primarily buoyancy driven and its variability can be well described by scaling parameters:

Length scalehVelocity scale $w_* = \left(\frac{ghH}{\rho c_p \theta_0}\right)^{1/3}$ Timescale $t_* = h/w_*$ Temperature scale $\theta_* = \frac{H}{\rho c_p w_*}$ 

for h the depth of the layer and H the surface heat flux



# **Towards stochastic parameterization**

- Lock in current 1.5km MetUM operational model:
  - adds perturbations  $\sim \theta_*$  with uniformly distributed random numbers
- Kober and Craig (2016) in 2.8km COSMO tests:
  - adds perturbations  $\sim \sqrt{\overline{\theta'^2}}$  and Gaussian bump style random number structure



# Limited number of large eddies

- Assume key source of variability is due to finite number of large eddies n averaged over in a given area
- The large eddies are independent and so Poisson
- Heating from each event warms area of  $\sim h^2$  by amount  $\sim heta_*$  in time  $t_*$

$$\frac{\partial \theta}{\partial t}\Big|_{\rm BL} = \frac{n}{\overline{n}} \left. \frac{\partial \theta}{\partial t} \right|_{\rm det} \qquad ; \qquad \overline{n} = \frac{\Delta x \Delta y \Delta t}{h^2 t_*}$$

Very shortly to be tested in MetUM (Clark et al)



#### Summary

- Spatial averaging  $\neq$  ensemble averaging for  $l \sim \Delta$
- If spatial average wanted, an important source of variability arises if the parameterized phenomenon includes important dynamical modes not much below the filter scale
- This occurs in convective parameterization context ("not enough clouds in the grid box")
- It also occurs in convection-permitting models in respect of the parameterized BL turbulence
- Simple stochastic noise can systematically affect initiation of deep convective clouds in such models
- Schemes now being explored that can account for turbulent variability and filter size  $\Delta$  in a natural way



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#### **Extras: if time and interest**



## **Upscaling of perturbations**

 One-off stochastic boundary-layer perturbation after 15 h, produces 500 hPa geopential simulations synoptic scale in 2.8 km large-domain COSMO simulation (right).



- Stochastic convection scheme in 28 km model is effective in capturing this upscale growth (centre, Plant-Craig).
- Deterministic scheme has very weak response (right, Tiedtke) as intended for an ensemble-mean parameterization method



## **Convective regime frequencies**

Timescale,  $\tau_c = CAPE/(dCAPE/dt)$  due to convection)



